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A geometric approach to multi-modal and multi-agent systems

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A geometric approach to multi-modal and multi-agent systems

From disturbance decoupling to consensus

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